

prove that

$$A \times (B \cap C) = (A \times B) \cap (A \times C)$$

sol

$$\begin{aligned} (a, b) \in (A \times (B \cap C)) &\Rightarrow a \in A \wedge b \in (B \cap C) \Rightarrow a \in A \wedge (b \in B \wedge b \in C) \\ &\Rightarrow (a, b) \in A \times B \wedge (a, b) \in A \times C \Rightarrow (a, b) \in (A \times B) \cap (A \times C) \\ &\Rightarrow A \times (B \cap C) \subseteq (A \times B) \cap (A \times C) \end{aligned} \quad (1)$$

$$\begin{aligned} (a, b) \in (A \times B) \cap (A \times C) &\Rightarrow (a, b) \in (A \times B) \wedge (a, b) \in (A \times C) \\ &\Rightarrow a \in A \wedge b \in B \wedge b \in C \Rightarrow a \in A \wedge b \in (B \cap C) \Rightarrow (a, b) \in A \times (B \cap C) \\ &\Rightarrow (A \times B) \cap (A \times C) \subseteq A \times (B \cap C) \end{aligned} \quad (2)$$

from (1) and (2) we get
 $A \times (B \cap C) = (A \times B) \cap (A \times C)$

لاحظ ان

$$(A \times B) = \{(a, b): a \in A \wedge b \in B\}$$

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